

Solutions to Test Review 4-3-17

1) binomial distribution $n = 400$ $p = 0.64$ $P(x < 340)$ MUST ADJUST because NO EQUALITY
 $P(0 \leq x \leq 339) = \text{binomCdf}(400, 0.64, 0, 339) \approx 1.$

2) binomial distribution $n = 600$ $p = 0.45$ $P(x \leq 305)$ NO ADJUST because EQUALITY
 $P(0 \leq x \leq 305) = \text{binomCdf}(600, 0.45, 0, 305) \approx 0.99817$

3) binomial distribution $n = 80$ $p = 0.75$ $P(x > 62)$ MUST ADJUST because NO EQUALITY
 $P(63 \leq x \leq 80) = \text{binomCdf}(80, 0.75, 63, 80) \approx 0.263575$

normal distribution $n = 80$ $p = 0.75$ $P(x > 62)$

MUST ADJUST because approximating BINOMIAL

$$\text{mean} = 80 \cdot 0.75 \rightarrow 60. \quad \text{SD} = \sqrt{80 \cdot 0.75 \cdot 0.25} \rightarrow 3.87298$$

$$P(62.5 \leq x \leq 80.5) = \text{normCdf}(62.5, 80.5, 60, 3.8730) \approx 0.259303$$

4) binomial distribution $n = 20$ $p = 0.56$ $P(x=9)$ MUST ADJUST because NO EQUALITY

$$P(x=9) = \text{binomPdf}(20, 0.56, 9) \approx 0.108862$$

normal distribution $n = 20$ $p = 0.56$ $P(8.5 < x < 9.5)$

MUST ADJUST because approximating BINOMIAL

$$\text{mean} = 20 \cdot 0.56 \rightarrow 11.2 \quad \text{SD} = \sqrt{20 \cdot 0.56 \cdot 0.44} \rightarrow 2.21991$$

$$P(8.5 \leq x \leq 9.5) = \text{normCdf}(8.5, 9.5, 11.2, 2.2199) \approx 0.109957$$

5) normal distribution mean = 500 SD = 50

usual range mean \pm 2SD

$$500 - 2(50) \text{ to } 500 + 2(50)$$

$$500 - 100 \text{ to } 500 + 100$$

$$400 \text{ to } 600$$

6) normal distribution mean =500 SD = 50

P(x<475) NO ADJUST necessary BECAUSE NORMAL

$$P(0 < x < 475) = \text{normCdf}(0, 475, 500, 50) = 0.308538$$

7) normal distribution mean =500 SD = 50

P(x>575) NO ADJUST necessary BECAUSE NORMAL

$$P(575 < x < 100000000) = \text{normCdf}(575, 100000000, 500, 50) = 0.066807$$

8) normal distribution mean =500 SD = 50

P(490<x<540) NO ADJUST necessary BECAUSE NORMAL

$$P(490 < x < 540) = \text{normCdf}(490, 540, 500, 50) = 0.367404$$

9) normal distribution mean =500 SD = 50

$$P(x < \text{LOW}) = 0.15 \quad \text{LOW} = \text{invNorm}(0.15, 500, 50) \rightarrow 448.178$$

The highest value is 448.178 kg

10) normal distribution mean =500 SD = 50

$$P(x > \text{HIGH}) = 0.20 \quad 1 - 0.20 = 0.80$$

$$\text{HIGH} = \text{invNorm}(0.8, 500, 50) \rightarrow 542.081$$

The highest value is 542.081 kg

11) binomial distribution n = 2000 p = 0.25 q = 1 - 0.25 = 0.75

P(480 ≤ x ≤ 505) NO BINOMIAL ADJUST BECAUSE EQUALITY

$$P(480 \leq x \leq 505) = \text{binomCdf}(2000, 0.25, 480, 505) \rightarrow 0.468552$$

$$\text{normal distribution mean} = 2000 \cdot 0.25 \rightarrow 500. \text{ SD} = \sqrt{2000 \cdot 0.25 \cdot 0.75} \rightarrow 19.3649$$

P(480 ≤ x ≤ 505) NORMAL ALWAYS ADJUSTS TO APPROXIMATE BINOMIAL

$$P(479.5 < x < 505.5) = \text{normCdf}(479.5, 505.5, 500, 19.3649) = 0.466915$$

12) binomial distribution n = 2000 p = 0.25 q = 1-0.25 = 0.75

P(x=502) NO BINOMIAL ADJUST BECAUSE EQUALITY

$$P(x=502)=\text{binomPdf}(2000,0.25,502) \rightarrow 0.020461$$

$$\text{normal distribution mean} = 2000 \cdot 0.25 \rightarrow 500. \text{ SD} = \sqrt{2000 \cdot 0.25 \cdot 0.75} \rightarrow 19.3649$$

P(x=502) NORMAL ALWAYS ADJUSTS TO APPROXIMATE BINOMIAL

$$P(501.5 < x < 502.5) = \text{normCdf}(501.5, 502.5, 500, 19.3649) = 0.020489$$

13) binomial distribution n = 2000 p = 0.25 q = 1-0.25 = 0.75

P(x<495) BINOMIAL ADJUST BECAUSE NO EQUALITY

$$P(0 \leq x \leq 494) = \text{binomCdf}(2000, 0.25, 0, 494) \rightarrow 0.389721$$

$$\text{normal distribution mean} = 2000 \cdot 0.25 \rightarrow 500. \text{ SD} = \sqrt{2000 \cdot 0.25 \cdot 0.75} \rightarrow 19.3649$$

P(0 ≤ x ≤ 494) NORMAL ALWAYS ADJUSTS TO APPROXIMATE BINOMIAL

$$P(-0.5 < x < 494.5) = \text{normCdf}(-0.5, 494.5, 500, 19.3649) = 0.388198$$

14) binomial distribution n = 2000 p = 0.25 q = 1-0.25 = 0.75

P(475< x < 520) BINOMIAL ADJUST BECAUSE NO EQUALITY

$$P(476 \leq x \leq 519) = \text{binomCdf}(2000, 0.25, 476, 519) \rightarrow 0.740596$$

$$\text{normal distribution mean} = 2000 \cdot 0.25 \rightarrow 500. \text{ SD} = \sqrt{2000 \cdot 0.25 \cdot 0.75} \rightarrow 19.3649$$

P(476 ≤ x ≤ 519) NORMAL ALWAYS ADJUSTS TO APPROXIMATE BINOMIAL

$$P(475.5 < x < 519.5) = \text{normCdf}(475.5, 519.5, 500, 19.3649) = 0.740123$$

15) binomial distribution n = 2000 p = 0.25 q = 1-0.25 = 0.75

P(x ≥ 496) NO BINOMIAL ADJUST BECAUSE EQUALITY

$$P(496 \leq x \leq 2000) = \text{binomCdf}(2000, 0.25, 496, 2000) \rightarrow 0.590291$$

$$\text{normal distribution mean} = 2000 \cdot 0.25 \rightarrow 500. \text{ SD} = \sqrt{2000 \cdot 0.25 \cdot 0.75} \rightarrow 19.3649$$

P(496 ≤ x ≤ 2000) NORMAL ALWAYS ADJUSTS TO APPROXIMATE BINOMIAL

$$P(495.5 < x < 2000.5) = \text{normCdf}(495.5, 2000.5, 500, 19.3649) = 0.591878$$

16A) FOR $np \geq 5$ to work we know $n=500$

$$500p \geq 5$$

$$\frac{500p}{500} \geq \frac{5}{500}$$

$$p \geq 0.01$$

✓✓ $500 \cdot 0.01 \rightarrow 5.$

16B) FOR $np < 5$ to work we know $p=0.13$

$$n(0.13) < 5$$

$$\frac{0.13p}{0.13} < \frac{5}{0.13}$$

$$p < 38.4615$$

$$p = 38$$

✓✓ $38 \cdot 0.13 \rightarrow 4.94$

$$P = \frac{\min + \max}{2} \quad E = \frac{\max - \min}{2}$$

17) given INTERVAL NOTATION (19.5,43.9)

$$p = \frac{19.5 + 43.9}{2} \rightarrow 31.7 \quad E = \frac{43.9 - 19.5}{2} \rightarrow 12.2$$

CONJUNCTION NOTATION $19.5 < p < 43.9$

TOLERANCE NOTATION 31.7 ± 12.2

18) given CONJUNCTION NOTATION $12.6 < p < 78.8$

$$p = \frac{12.6 + 78.8}{2} \rightarrow 45.7 \quad E = \frac{78.8 - 12.6}{2} \rightarrow 33.1$$

INTERVAL NOTATION (12.6,78.8)

TOLERANCE NOTATION 45.7 ± 33.1

$$P = \frac{\min + \max}{2} \quad E = \frac{\max - \min}{2}$$

19) $p = 75.45$ $E = 3.42$

$$\min = 75.45 - 3.42 = 72.03 \quad \max = 75.45 + 3.42 = 78.87$$

INTERVAL NOTATION $(72.03, 78.87)$

CONJUNCTION NOTATION $72.03 < p < 78.87$

TOLERANCE NOTATION 75.45 ± 3.42

20) given TOLERANCE NOTATION 79.8 ± 9.6

$$p = 79.8 \quad E = 9.6$$

$$\min = 79.8 - 9.6 = 70.2 \quad \max = 79.8 + 9.6 = 89.4$$

INTERVAL NOTATION $(70.2, 89.4)$

CONJUNCTION NOTATION $70.2 < p < 89.4$

21-27)

$$x = 175 \ n = 420 \ p = \frac{175}{420} \rightarrow 0.416667 \ q = 1 - \frac{175}{420} \rightarrow 0.583333$$

$$CL = 54\% = 0.54 \ ALPHA = 1 - 0.54 \rightarrow 0.46 \ \frac{1}{2}ALPHA = \frac{0.46}{2} \rightarrow 0.23$$

$$CV = \text{invNorm}(0.23) \rightarrow -0.738847 = 0.7388$$

$$E = 0.7388 \cdot \sqrt{\frac{0.4167 \cdot 0.5833}{420}} = 0.017773$$

$$\min \ 0.4167 - 0.0178 \rightarrow 0.3989 \quad \max \ 0.4167 + 0.0178 \rightarrow 0.4345$$

INTERVAL NOTATION $(0.3989, 0.4345)$

CONJUNCTION NOTATION $0.3989 < p < 0.4345$

TOLERANCE NOTATION 0.4167 ± 0.0178

28-34)

$$x = 954 \quad n = 1800 \quad p = \frac{954}{1800} \rightarrow 0.53 \quad q = 1 - \frac{954}{1800} \rightarrow 0.47$$

$$CL = 99\% \quad CV = 2.575$$

$$E = 2.575 \cdot \sqrt{\frac{0.53 \cdot 0.47}{1800}} = 0.030292$$

$$\text{min } 0.53 - 0.0303 \rightarrow 0.4997 \quad \text{max } 0.53 + 0.0303 \rightarrow 0.5603$$

INTERVAL NOTATION (0.4997, 0.5603)

CONJUNCTION NOTATION $0.4997 < p < 0.5603$

TOLERANCE NOTATION 0.53 ± 0.0303

$$35) p = 84.5\% = 0.845 \quad q = 1 - 0.845 = 0.155$$

$$CL = 78\% = 0.78 \quad ALPHA = 1 - 0.78 = 0.22 \quad \frac{1}{2}ALPHA = \frac{0.22}{2} = 0.11$$

$$CV = \text{invNorm}(0.11) \rightarrow -1.22653 \quad E = 0.028$$

$$n = \frac{CV^2 pq}{E^2} = \frac{(1.2265)^2 \cdot 0.845 \cdot 0.155}{(0.028)^2} = 251.309 \quad \text{ROUND UP TO 252}$$

$$36) p = 5.4\% = 0.054 \quad q = 1 - 0.054 = 0.946$$

$$CL = 99\% \quad CV = 2.575 \quad E = 0.084$$

$$n = \frac{CV^2 pq}{E^2} = \frac{(2.575)^2 \cdot 0.054 \cdot 0.946}{(0.084)^2} = 48.0044 \quad \text{ROUND UP TO 49}$$

37) p = ???

$$CL = 72\% = 0.72 \quad ALPHA = 1 - 0.72 = 0.28 \quad \frac{1}{2}ALPHA = \frac{0.28}{2} = 0.14$$

$$CV = \text{invNorm}(0.14) \rightarrow -1.08032 \quad E = 0.084$$

$$n = \frac{CV^2 pq}{E^2} = \frac{(1.08)^2 \cdot 0.25}{(0.084)^2} = 41.3265 \quad \text{ROUND UP TO 42}$$

38) p = ???

$$CL = 90\% \quad CV = 1.645 \quad E = 0.04$$

$$n = \frac{CV^2 pq}{E^2} = \frac{(1.645)^2 \cdot 0.25}{(0.04)^2} = 422.816 \quad \text{ROUND UP TO 423}$$