

Problem 2

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
	A1 x

$x=12 \quad n=56 \quad p=12/56 = \frac{3}{14} \approx 0.214286 \quad q=1-0.214286 = 0.785714$

confidence level = 95. % = 0.95 alpha = 0.05 $\frac{\alpha}{2} = 0.025$

$CV = z_{0.5\alpha} = \text{invnorm}(0.025, 0, 1) = \pm 1.95996$

Margin of Error

$$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$$
$$= 1.95996 \sqrt{[(0.214286)(0.785714)]/56}$$
$$\approx 0.107469$$

confidence level =95. % =0.95 alpha =0.05 $\frac{\alpha}{2} = 0.025$

p =0.214286 E≈0.107469

confidence interval for p

We are 95. % confident that "p" lies in the following interval
interval notation

$$(p-E, p+E) = (0.214286 - 0.107469, 0.214286 + 0.107469) \\ = (0.106817, 0.321755)$$

conjunction notation

$$p-E < p < p+E \quad 0.214286 - 0.107469 < p < 0.214286 + 0.107469 \\ 0.106817 < p < 0.321755$$

tolerance notation 0.214286 ± 0.107469

Problem 3

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
	A1 x

$$x=12 \quad n=20 \quad p=12/20 = \frac{3}{5} \approx 0.6 \quad q=1-0.6 = 0.4$$

$$\text{confidence level } = 95\% = 0.95 \quad \text{alpha } = 0.05 \quad \frac{\text{alpha}}{2} = 0.025$$

$$CV = z_{0.5\alpha} = \text{invnorm}(0.025, 0, 1) = \pm 1.95996$$

Margin of Error

$$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$$

$$= 1.95996 \sqrt{[(0.6)(0.4)/20]}$$

$$\approx 0.214703$$

confidence level =95. % =0.95 alpha =0.05 $\frac{\alpha}{2} = 0.025$

p =0.6 E≈0.214703

confidence interval for p

We are 95. % confident that "p" lies in the following interval
interval notation

$$(p-E, p+E) = (0.6 - 0.214703, 0.6 + 0.214703) \\ = (0.385297, 0.814703)$$

conjunction notation

$$p-E < p < p+E \quad 0.6 - 0.214703 < p < 0.6 + 0.214703 \\ 0.385297 < p < 0.814703$$

tolerance notation 0.6 ± 0.214703

Problem 4

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
A1	x

$x=15 \quad n=90 \quad p=15/90 = \frac{1}{6} \approx 0.166667 \quad q=1-0.166667 = 0.833333$

confidence level = 90. % = 0.9 alpha = 0.1 $\frac{\alpha}{2} = 0.05$

$CV = z_{0.5\alpha} = \text{invnorm}(0.05, 0, 1) = \pm 1.64485$

Margin of Error

$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$

$= 1.64485 \sqrt{[(0.166667)(0.833333)]/90}$

≈ 0.064616

confidence level =90. % =0.9 alpha =0.1 $\frac{\alpha}{2} = 0.05$

p =0.166667 E≈0.064616

confidence interval for p

We are 90. % confident that "p" lies in the following interval
interval notation

$$(p-E, p+E) = (0.166667 - 0.064616, 0.166667 + 0.064616) \\ = (0.102051, 0.231283)$$

conjunction notation

$$p-E < p < p+E \quad 0.166667 - 0.064616 < p < 0.166667 + 0.064616 \\ 0.102051 < p < 0.231283$$

tolerance notation 0.166667 ± 0.064616

Problem 5

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
A1	x

$x=18 \quad n=45 \quad p=18/45 = \frac{2}{5} \approx 0.4 \quad q=1-0.4 = 0.6$

confidence level = 99. % = 0.99 alpha = 0.01 $\frac{\alpha}{2} = 0.005$

$CV = z_{0.5\alpha} = \text{invnorm}(0.005, 0, 1) = \pm 2.57583$

Margin of Error

$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$

$= 2.57583 \sqrt{[(0.4)(0.6)/45]}$

≈ 0.188112

confidence level =99. % =0.99 alpha =0.01 $\frac{\alpha}{2} = 0.005$

p =0.4 E≈0.188112

confidence interval for p

We are 99. % confident that "p" lies in the following interval
interval notation

$$(p-E, p+E) = (0.4 - 0.188112, 0.4 + 0.188112) \\ = (0.211888, 0.588112)$$

conjunction notation

$$p-E < p < p+E \quad 0.4 - 0.188112 < p < 0.4 + 0.188112 \\ 0.211888 < p < 0.588112$$

tolerance notation 0.4±0.188112

Problem 6

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
A1	x

$x=25 \quad n=500 \quad p=25/500 = \frac{1}{20} \approx 0.05 \quad q=1-0.05 = 0.95$

confidence level = 75. % = 0.75 alpha = 0.25 $\frac{\alpha}{2} = 0.125$

$CV = z_{0.5\alpha} = \text{invnorm}(0.125, 0, 1) = \pm 1.15035$

Margin of Error

$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$

$= 1.15035 \sqrt{[(0.05)(0.95)]/500}$

≈ 0.011212

confidence level = 75% = 0.75 alpha = 0.25 $\frac{\alpha}{2} = 0.125$

p = 0.05 E ≈ 0.011212

confidence interval for p

We are 75% confident that "p" lies in the following interval
interval notation

$$\begin{aligned}(p-E, p+E) &= (0.05 - 0.011212, 0.05 + 0.011212) \\ &= (0.038788, 0.061212)\end{aligned}$$

conjunction notation

$$\begin{aligned}p-E < p < p+E \quad 0.05 - 0.011212 < p < 0.05 + 0.011212 \\ 0.038788 < p < 0.061212\end{aligned}$$

tolerance notation 0.05 ± 0.011212

Problem 7

	A
=	
1	x
2	n
3	conf level
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5	
6	
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8	
9	
10	
11	
A1	x

$x=12 \quad n=200 \quad p=12/200 = \frac{3}{50} \approx 0.06 \quad q=1-0.06 = 0.94$

confidence level = 64. % = 0.64 alpha = 0.36 $\frac{\alpha}{2} = 0.18$

$CV = z_{0.5\alpha} = \text{invnorm}(0.18, 0, 1) = \pm 0.915365$

Margin of Error

$$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$$
$$= 0.915365 \sqrt{[(0.06)(0.94)/200]}$$
$$\approx 0.015372$$

confidence level = $64.$ %= 0.64 alpha = 0.36 $\frac{\alpha}{2} = 0.18$

p = 0.06 E ≈ 0.015372

confidence interval for p

We are $64.$ % confident that "p" lies in the following interval
interval notation

$$(p-E, p+E) = (0.06 - 0.015372, 0.06 + 0.015372) \\ = (0.044628, 0.075372)$$

conjunction notation

$$p-E < p < p+E \quad 0.06 - 0.015372 < p < 0.06 + 0.015372 \\ 0.044628 < p < 0.075372$$

tolerance notation 0.06 ± 0.015372

Problem 8

	A
=	
1	x
2	n
3	conf level
4	
5	
6	
7	
8	
9	
10	
11	
A1	x

$x=48 \quad n=500 \quad p=48/500 = \frac{12}{125} \approx 0.096 \quad q=1-0.096 = 0.904$

confidence level = 85. % = 0.85 alpha = 0.15 $\frac{\alpha}{2} = 0.075$

$CV = z_{0.5\alpha} = \text{invnorm}(0.075, 0, 1) = \pm 1.43953$

Margin of Error

$$E = CV \cdot \sqrt{\frac{p \cdot q}{n}}$$
$$= 1.43953 \sqrt{[(0.096)(0.904)/500]}$$
$$\approx 0.018965$$

$$\text{confidence level} = 85. \% = 0.85 \quad \alpha = 0.15 \quad \frac{\alpha}{2} = 0.075$$

$$p = 0.096 \quad E \approx 0.018965$$

confidence interval for p

We are 85. % confident that "p" lies in the following interval
interval notation

$$(p - E, p + E) = (0.096 - 0.018965, 0.096 + 0.018965) \\ = (0.077035, 0.114965)$$

conjunction notation

$$p - E < p < p + E \quad 0.096 - 0.018965 < p < 0.096 + 0.018965 \\ 0.077035 < p < 0.114965$$

tolerance notation 0.096 ± 0.018965