

Problem 1

- 1) False Normal Distribution typically deals with ranges of values or strict inequalities
- 2) False if $np < 5$ or $nq < 5$, then you cannot use normal distribution to approximate binomial
- 3) True this is the continuity correction factor add 0.5 to max boundary and subtract 0.5 from min boundary
- 4) False, unlike binomial $P(x < 2)$ and $P(x \leq 2)$ are the same
- 5) $np \geq 5$
- 6) $nq \geq 5$

Normally Distributed melon weights

mean = 1.8 SD = 0.3

7) usual range is within 2 standard deviations of mean

$$1.8 - 2 \cdot 0.3 \blacktriangleright 1.2 \qquad 1.8 + 2 \cdot 0.3 \blacktriangleright 2.4$$

these melons will typically run from 1.2 kg to 2.4 kg

8) $P(x > 2) \text{ normCdf}(2, 1000000, 1.8, 0.3) = 0.252492$

9) $P(x < 1.75) \text{ normCdf}(0, 1.75, 1.8, 0.3) = 0.433816$

10) $P(1.6 < x < 1.9) \text{ normCdf}(1.6, 1.9, 1.8, 0.3) = 0.378066$

11a) lowest 19% weight $X_{\text{low}} = \text{invNorm}(0.19, 1.8, 0.3) \blacktriangleright 1.53663$

11b) highest 24% weight $X_{\text{high}} = \text{invNorm}(0.76, 1.8, 0.3) \blacktriangleright 2.01189$

11) the acceptable range of melons for this specialized grocery store is 1.567 kg to 2.012 kg

12) $N = 56$ $p = 0.3$

Find $P(12) = P(x=12)$

binomial $\text{binomPdf}(56, 0.3, 12) \rightarrow 0.045363$

for normal we need to find some things first

$np = 56 \cdot 0.3 \rightarrow 16.8$ (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.3 \rightarrow 0.7$ (since $nq = 56 \cdot 0.7 = 39.2$ and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{56 \cdot 0.3 \cdot 0.7} \rightarrow 3.42929$

now we can build a macro to find $P(x=12)$

normal $\text{normCdf}(11.5, 12.5, 16.8, 3.429) \rightarrow 0.043823$

13) $N = 56$ $p = 0.03$

Find $P(x < 17) = P(x \leq 16)$

binomial `binomCdf(56,0.03,0,16)` ▶ 1.

for normal we need to find some things first

$np = 56 \cdot 0.03$ ▶ 1.68

since np is NOT larger than 5,
we can't use normal to
approximate binomial

14) $N = 56$ $p = 0.09$

Find $P(x > 5) = P(x \geq 6)$

binomial $\text{binomCdf}(56, 0.09, 6, 1000000) \rightarrow 0.391268$

for normal we need to find some things first

$np = 56 \cdot 0.09 \rightarrow 5.04$ (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.09 \rightarrow 0.91$ (since $nq = 56 \cdot 0.91 = 50.96$ and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{56 \cdot 0.09 \cdot 0.91} \rightarrow 2.14159$

now we can build a macro to find $P(x > 6)$

normal $\text{normCdf}(5.5, 100000, 5.04, 2.142) \rightarrow 0.41498$

$n = 100$ $p = 0.80$

15) find $P(x=75)$ or $P(75)$

binomial $\text{binomPdf}(100, 0.8, 75) \triangleright 0.043878$

for normal we need to find some things first

$np = 100 \cdot 0.8 \triangleright 80$. (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.8 \triangleright 0.2$ (since $nq = 100 \cdot 0.2 = 20$. and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{100 \cdot 0.8 \cdot 0.2} \triangleright 4$.

now we can build a macro to find $P(x=75)$

normal $\text{normCdf}(74.5, 75.5, 80, 4) \triangleright 0.045729$

$n = 100$ $p = 0.80$

16) find $P(x \leq 78)$

binomial $\text{binomCdf}(100, 0.8, 0, 78) \rightarrow 0.345967$

for normal we need to find some things first

$np = 100 \cdot 0.8 \rightarrow 80$. (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.8 \rightarrow 0.2$ (since $nq = 100 \cdot 0.2 = 20$. and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{100 \cdot 0.8 \cdot 0.2} \rightarrow 4$.

now we can build a macro to find $P(x \leq 78)$

normal $\text{normCdf}(-0.5, 78.5, 80, 4) \rightarrow 0.35383$

$n = 100$ $p = 0.80$

17) find $P(x > 77) = P(x \geq 78)$

binomial $\text{binomCdf}(100, 0.8, 78, 100) \blacktriangleright 0.738933$

for normal we need to find some things first

$np = 100 \cdot 0.8 \blacktriangleright 80$. (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.8 \blacktriangleright 0.2$ (since $nq = 100 \cdot 0.2 = 20$. and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{100 \cdot 0.8 \cdot 0.2} \blacktriangleright 4$.

now we can build a macro to find $P(x \leq 78)$

normal $\text{normCdf}(77.5, 100.5, 80, 4) \blacktriangleright 0.734014$

$n = 100$ $p = 0.80$

17) find $P(70 \leq x \leq 81)$

binomial $\text{binomCdf}(100, 0.8, 70, 81) \rightarrow 0.631854$

for normal we need to find some things first

$np = 100 \cdot 0.8 \rightarrow 80$. (since this is larger than 5, we can use normal to approximate)

$q = 1 - 0.8 \rightarrow 0.2$ (since $nq = 100 \cdot 0.2 = 20$. and nq larger than 5 we can use normal to approximate)

$SD = \sqrt{100 \cdot 0.8 \cdot 0.2} \rightarrow 4$.

now we can build a macro to find $P(x \leq 78)$

normal $\text{normCdf}(69.5, 81.5, 80, 4) \rightarrow 0.641837$