

## Problem 1

### Problems 1–7

$N = 4$  (four pack of energy drink)

$p = 0.032$  (probability there will be more than number of ounces on the can)

$q = 1 - 0.032 \rightarrow 0.968$

1) Model  $P(x) = nCr(4,x) \cdot 0.032^x \cdot 0.968^{4-x}$

Model  $P(x)$  `binompdf(4,0.032,x)`

2) table

`binomPdf(4,0.032)`  $\rightarrow \{0.878014, 0.116101, 0.005757, 0.000127, 0.000001\}$

3)  $P(x=1) = \text{binomPdf}(4,0.032,1) \rightarrow 0.116101$

4)  $P(x>2) = P(x \geq 3) = P(3 \leq x \leq 4) = \text{binomCdf}(4,0.032,3,4) \rightarrow 0.000128$

5)  $P(x \leq 3) = P(0 \leq x \leq 3) = \text{binomCdf}(4,0.032,0,3) \rightarrow 0.999999 \approx 1$

6)  $P(1 < x \leq 3) = P(2 \leq x \leq 3) = \text{binomCdf}(4,0.032,2,3) \rightarrow 0.005884$

7)  $p$  becomes  $q$

Model  $P(x) = nCr(4,x) \cdot 0.968^x \cdot 0.032^{4-x}$

Model  $P(x)$  `binompdf(4,0.968,x)`

## Problems 8–13

N = 6 (six bags of M&Ms)

p = 0.1224 (probability there will be less than 14 M&Ms in the bag)

q = 1 - 0.1224 ▶ 0.8776

$$8) \text{ Model } P(x) = \sum_{i=low}^{high} \left( nCr(6,i) \cdot 0.1224^i \cdot 0.8776^{6-i} \right)$$

Model P(x) binomCdf(6,0.1224,low, high)

9) table

binomCdf(6,0.1224) ▶ { 0.456856, 0.839166, 0.97247, 0.997259, 0.999852, 0.999997, 1. }

10) P(x=4) = binomPdf(6,0.1224,4) ▶ 0.002593

11) P(x<4) = P(x≤3) = P(0≤x≤3) = binomCdf(6,0.1224,0,3) ▶ 0.997259

12) P(x≥3) = P(3≤x≤6) = binomCdf(6,0.1224,3,6) ▶ 0.02753

13) P(2<x≤5) = P(3≤x≤5) = binomCdf(6,0.1224,3,5) ▶ 0.027527

Problem 2

14)  $n=12$   $p=0.5$ (heads)  $P(x<5)=P(0\leq x\leq 4) = \text{binomCdf}(12,0.5,0,4) \blacktriangleright 0.193848$

15)  $n=31$   $p=0.12$  (will snow)  $P(x\geq 3) = P(3\leq x\leq 31) = \text{binomCdf}(31,0.12,3,31) \blacktriangleright 0.736268$

16)  $n=50$   $p=0.48$  (dislike high school)  $P(x=12) = \text{binomPdf}(50,0.48,12) \blacktriangleright 0.000293$

17)  $n=24$   $p=0.35$  (die)

this asks about saplings that live so  $p$  changes to 0.65

$n=24$   $p=0.65$ (live)  $P(x\geq 15) = P(15\leq x\leq 24) = \text{binomCdf}(24,0.65,15,24) \blacktriangleright 0.68665$

18)  $n=12$   $p=0.10$  (faulty water bottles)  $P(x\leq 2) = P(0\leq x\leq 2) = \text{binomCdf}(12,0.1,0,2) \blacktriangleright 0.88913$

19)  $n=50$   $p=0.028$  (faulty ties)  $P(x=5) = \text{binomPdf}(50,0.028,5) \blacktriangleright 0.010159$

Problem 3

20)  $n = 11$   $p = 0.97$  (falling bottles) BUT this problem asked about NOT falling bottles

$n = 11$   $p = 0.03$  (NOT falling bottles)

$$P(x > 5) = P(x \geq 6) = P(6 \leq x \leq 11) = \text{binomCdf}(11, 0.03, 6, 11) \blacktriangleright 2.95709\text{E-}7 \approx 0.0000$$

21)  $n = 8$   $p = 0.008$  (defective component)

$P(\text{not working perfectly}) = P(x > 0) = P(x \geq 1)$

$$= P(1 \leq x \leq 8) = \text{binomCdf}(8, 0.008, 1, 8) \blacktriangleright 0.062236$$

22)  $n = 8$   $p = 0.008$  (defective component)

$P(\text{working perfectly}) = P(x = 0) = \text{binomPdf}(8, 0.008, 0) \blacktriangleright 0.937764$

23)  $n = 58$   $p = 0.10$  (defective toy)

$$P(x = 10) = \text{binomPdf}(58, 0.1, 10) \blacktriangleright 0.0332$$

24)  $n = 50$   $p = 0.79$  (from the state) BUT this problem asked about NOT from state

$n = 50$   $p = 0.21$  (NOT from state)

$$P(x > 3) = P(x \geq 4) = P(4 \leq x \leq 50) = \text{binomCdf}(50, 0.21, 4, 50) \blacktriangleright 0.996431$$

Problem 4

25-32  $n = 5$   $p = \text{????}$  (must use table)

25) find  $q$

$$1 = 0.2486 + 0.399 + 0.2562 + 0.0132 + 0.0008 + q$$

$$1 = q + 0.9178$$

$$q = 1 - 0.9178 = 0.0822$$

	A	B	C	D
=				
1	x	p(x)		
2		0	0.2486	
3		1	0.399	
4		2	0.2562	
5		3	q	0.0822
6		4	0.0132	
7		5	0.0008	
8				
9				
10				
11				
C8				

25-32  $n = 5$   $p = \text{????}$  (must use table)

26) Complete Cumulative distribution table

$c_p(0) = 0.2486$  (always same)

$c_p(1) = 0.2486 + 0.399 \rightarrow 0.6476$

$c_p(2) = 0.2486 + 0.399 + 0.2562 \rightarrow 0.9038$

$c_p(3) = 0.2486 + 0.399 + 0.2562 + 0.0822 \rightarrow 0.986$

$c_p(4) = 0.2486 + 0.399 + 0.2562 + 0.0822 + 0.0132 \rightarrow 0.9992$

$c_p(5) = 0.2486 + 0.399 + 0.2562 + 0.0822 + 0.0132 + 0.0008 = 1$

NOTE the LAST entry is the ONLY entry that can ever be 1 exactly!

	A	B	C	D
=				
1	x	p(x)	$c_p(x)$	
2		0	0.2486	0.2486
3		1	0.399	0.6476
4		2	0.2562	0.9038
5		3	0.0822	0.986
6		4	0.0132	0.9992
7		5	0.0008	1.
8				
9				
10				
11				
C2	0.2486			

25-32  $n = 5$   $p = ???? (must use table)$

$$27) P(2 \leq x \leq 4) = P(2) + P(3) + P(4)$$

$$= 0.2562 + 0.0822 + 0.0132 \rightarrow 0.3516$$

$$28) P(0 \leq x \leq 3) = P(0) + P(1) + P(2) + P(3)$$

$$= 0.2486 + 0.399 + 0.2562 + 0.0822 \rightarrow 0.986$$

OR this is in the cumulative distribution chart

$$29) P(1 < x < 5) = P(2 \leq x \leq 4)$$

$$= P(2) + P(3) + P(4)$$

$$= 0.2562 + 0.0822 + 0.0132 \rightarrow 0.3516$$

$$30) P(2 < x < 5) = P(3 \leq x \leq 4)$$

$$= P(3) + P(4)$$

$$= 0.0822 + 0.0132 \rightarrow 0.0954$$

	A	B	C	D
=				
1	x	p(x)	c_p(x)	
2		0	0.2486	0.2486
3		1	0.399	0.6476
4		2	0.2562	0.9038
5		3	0.0822	0.986
6		4	0.0132	0.9992
7		5	0.0008	1.
8				
9				
10				
11				
D5				

25-32  $n = 5$   $p = \text{????}$  (must use table)

$$\begin{aligned} 31) P(0 < x \leq 3) &= P(1 \leq x \leq 3) \\ &= P(1) + P(2) + P(3) \\ &= 0.399 + 0.2562 + 0.0822 \rightarrow 0.7374 \end{aligned}$$

$$\begin{aligned} 32) P(2 \leq x < 4) &= P(2 \leq x \leq 3) \\ &= P(2) + P(3) \\ &= 0.2562 + 0.0822 \rightarrow 0.3384 \end{aligned}$$

	A	B	C	D
=				
1	x	p(x)	c_p(x)	
2	0	0.2486	0.2486	
3	1	0.399	0.6476	
4	2	0.2562	0.9038	
5	3	0.0822	0.986	
6	4	0.0132	0.9992	
7	5	0.0008	1.	
8				
9				
10				
11				



33) Find w

Easiest way to find w

$$0.9966 + 0.0032 \rightarrow 0.9998$$

Another way to find

$$w = 1 - 0.0002 = 0.9998$$

	A	B	C	D	E
=					
1	x	p(x)	c_p(x)		
2	0	0.4011	0.4011		
3	1	0.402	0.8031		
4	2	0.1612	0.9643		
5	3	0.0323	0.9966		
6	4	0.0032	w	0.9998	
7	5	0.0002	1		
8					
9					
10					
11					