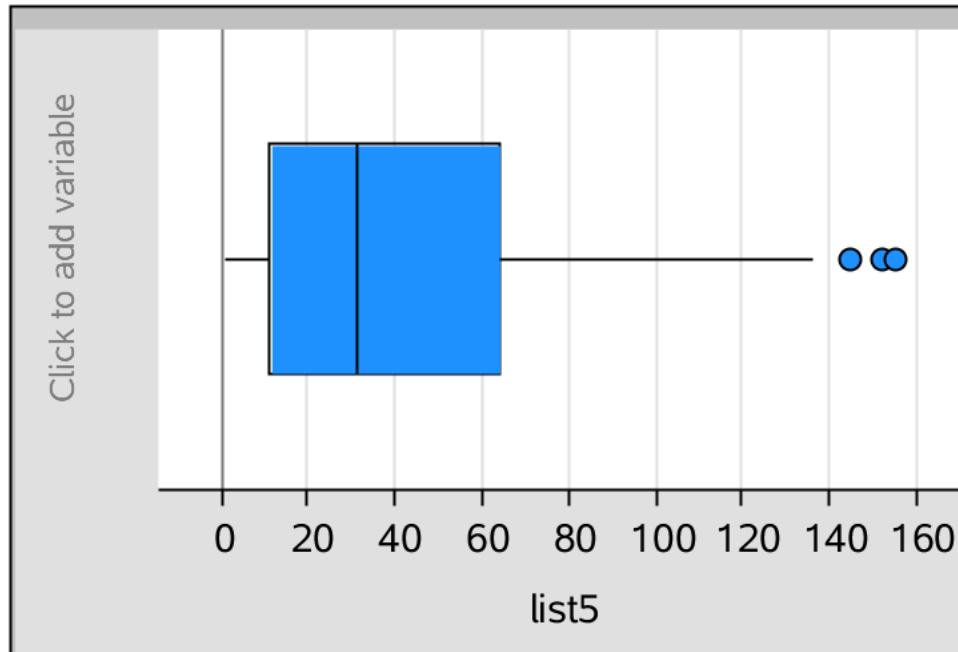


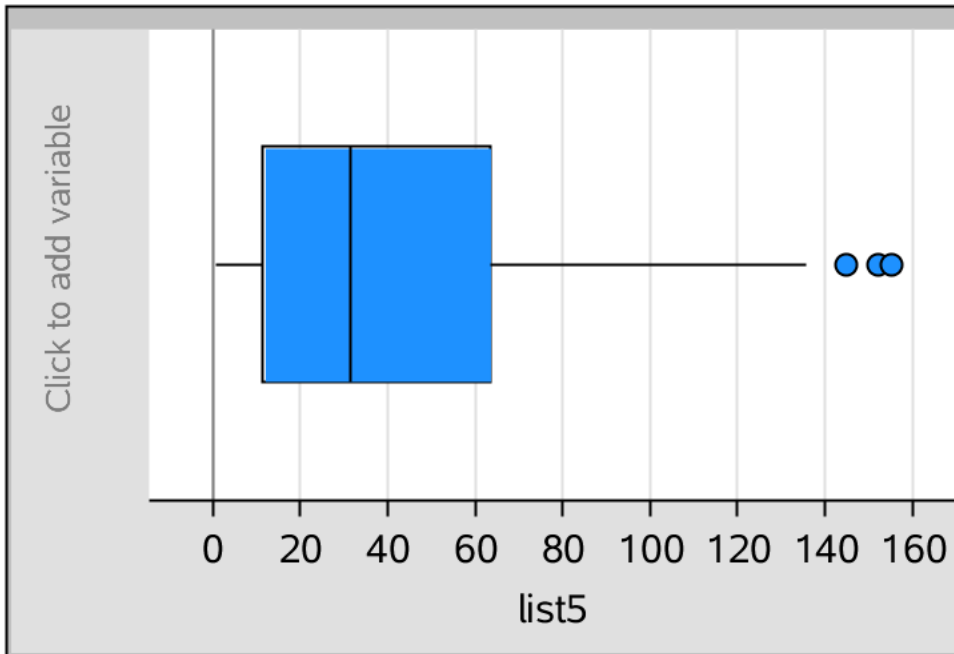
list5



	A list5	B	C	D
=			=OneVar(	
3	1	$\Sigma x$	1868.	
4	1	$\Sigma x^2$	171510.	
5	1	$s_x := s_{n-...}$	46.4853	
6	1	$\sigma_x := \sigma_{n...}$	45.9005	
7	1	n	40.	
8	2	MinX	1.	
9	2	$Q_1X$	11.5	
10	2	MedianX...	31.5	
11	21	$Q_3X$	64.	
12	22	MaxX	155.	
13	23	$SSX := \Sigma..$	84274.4	
A3	=1			

population variance =  $\frac{84274.4}{40.}$  ▶ 2106.86

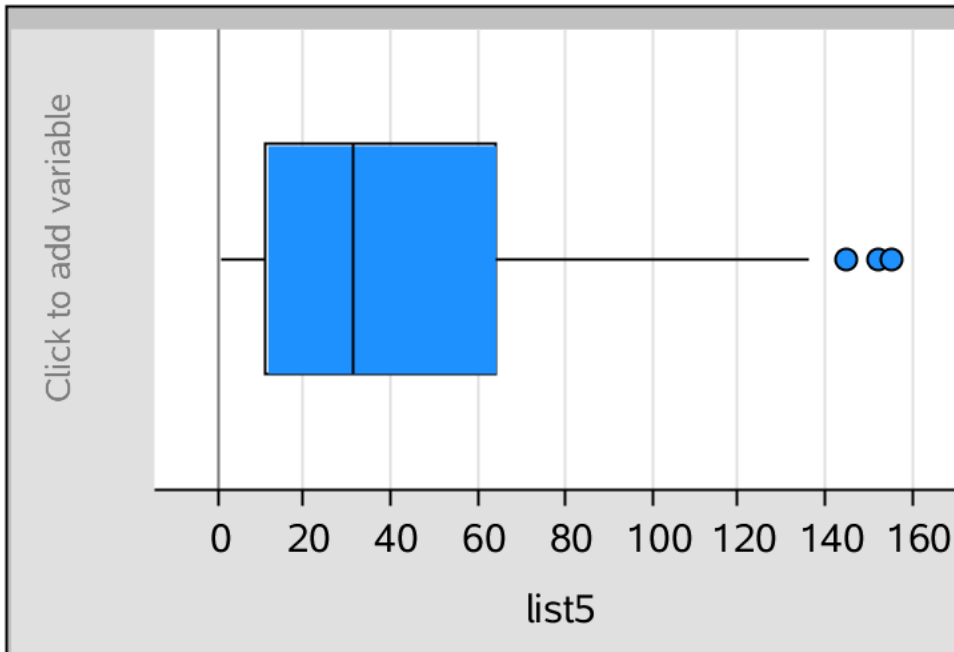
sample variance =  $\frac{84274.4}{39.}$  ▶ 2160.88



population st dev =  $\sqrt{\frac{84274.4}{40.}}$  ▶ 45.9005

sample st dev =  $\sqrt{\frac{84274.4}{39.}}$  ▶ 46.4853

	A list5	B	C	D
=			=OneVar(	
1		1 Title	One-Va...	
2		1 $\bar{x}$	46.7	
3		1 $\Sigma x$	1868.	
4		1 $\Sigma x^2$	171510.	
5		1 $s_x := s_{n-...}$	46.4853	
6		1 $\sigma_x := \sigma_{n...}$	45.9005	
7		1 n	40.	
8		2 MinX	1.	
9		2 $Q_1X$	11.5	
10		2 MedianX...	31.5	
11		21 $Q_3X$	64.	
A4	=1			



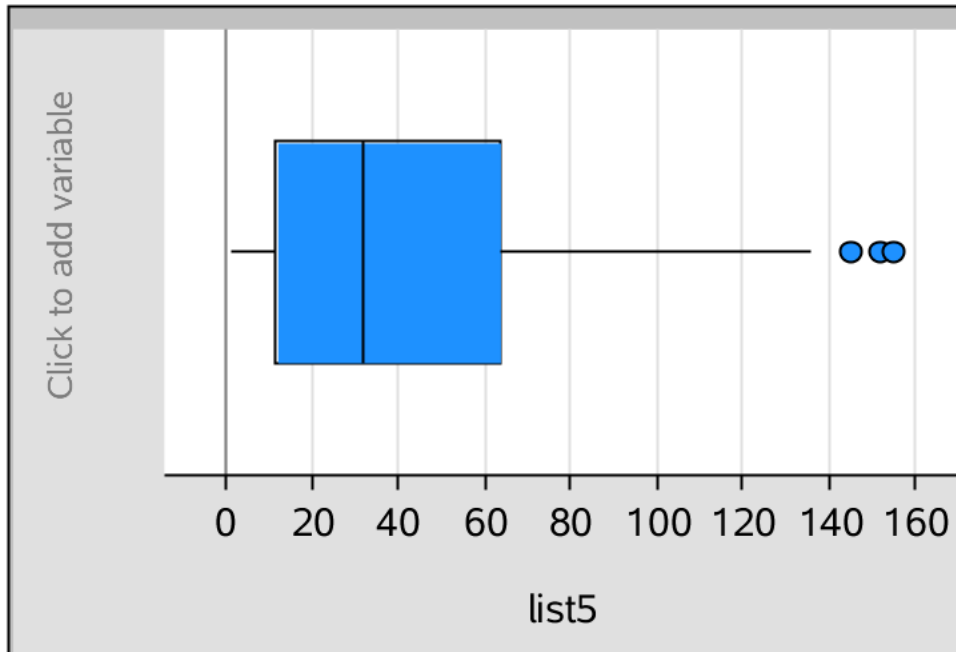
IQR =  $64 - 11.5$  ▶  $52.5$

Q1 score 11.5

Q3 score 64

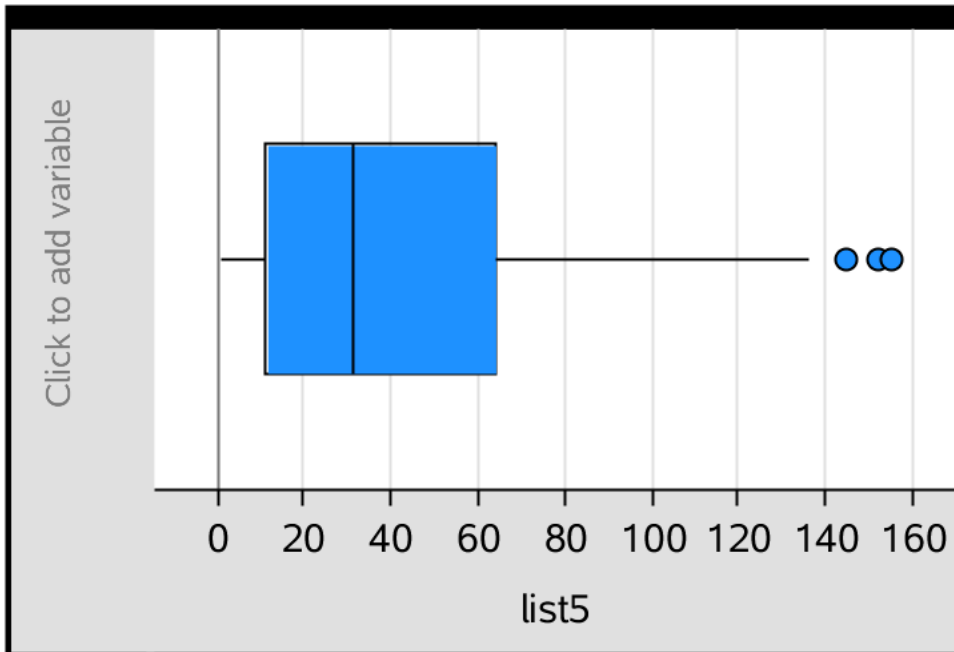
$1.5 \cdot \text{IQR} = 1.5 \cdot 52.5$  ▶  $78.75$

	A list5	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	46.7	
3	1	$\Sigma x$	1868.	
4	1	$\Sigma x^2$	171510.	
5	1	$s_x := s_{n-...}$	46.4853	
6	1	$\sigma_x := \sigma_{n...}$	45.9005	
7	1	n	40.	
8	2	MinX	1.	
9	2	$Q_1 X$	11.5	
10	2	MedianX...	31.5	
11	21	$Q_3 X$	64.	
A1	=1			



lower fence =  $11.5 - 78.75 = -67.25$   
 upper fence  $64 + 78.75 = 142.75$   
 all scores that lie  
 below  $x = -67.25$   
 and above  $x = 142.75$  are outliers  
 list 5 outliers 145 152 155

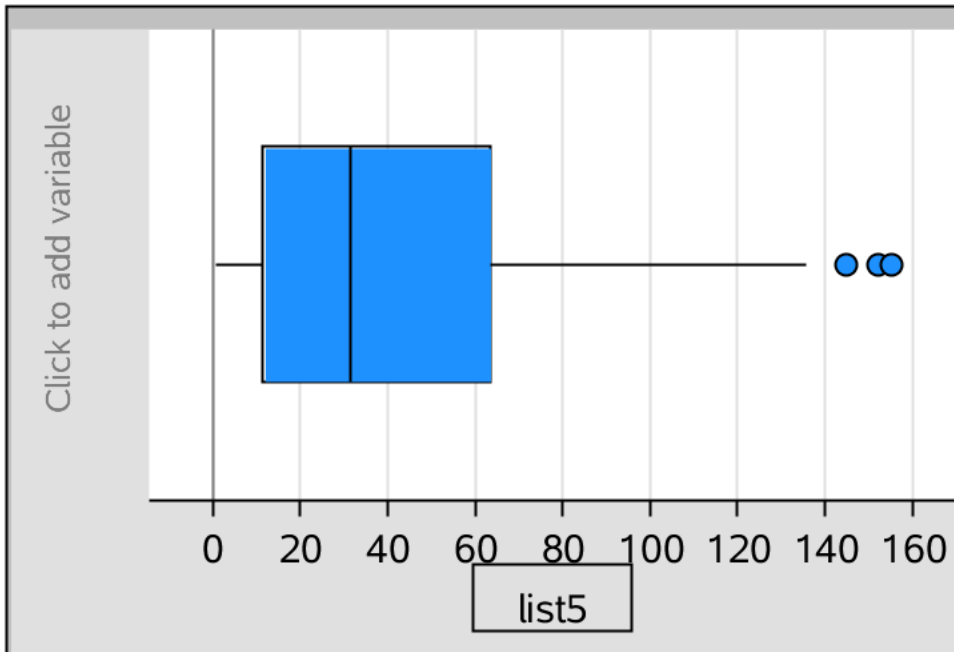
	A list5	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	46.7	
3	1	$\Sigma x$	1868.	
4	1	$\Sigma x^2$	171510.	
5	1	$s_x := s_{n-...}$	46.4853	
6	1	$\sigma_x := \sigma_{n...}$	45.9005	
7	1	n	40.	
8	2	MinX	1.	
9	2	$Q_1 X$	11.5	
10	2	MedianX...	31.5	
11	21	$Q_3 X$	64.	
A1	=1			



	A list5	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	46.7	
3	1	$\Sigma x$	1868.	
4	1	$\Sigma x^2$	171510.	
5	1	$s_x := s_{n-...}$	46.4853	
6	1	$\sigma_x := \sigma_{n...}$	45.9005	
7	1	n	40.	
8	2	MinX	1.	
9	2	$Q_1 X$	11.5	
10	2	MedianX...	31.5	
11	21	$Q_3 X$	64.	
<div style="border: 1px solid black; padding: 2px;">A1 = 1</div>				

all scores that lie  
below  $x = -67.25$  and  
above  $x = 142.75$  are outliers

list 5 outliers are 145, 152, and 155



	A list5	B	C	D
=			=OneVar(	
2	1	$\bar{x}$	46.7	
3	1	$\Sigma x$	1868.	
4	1	$\Sigma x^2$	171510.	
5	1	$s_x := s_{n-...}$	46.4853	
6	1	$\sigma_x := \sigma_{n...}$	45.9005	
7	1	n	40.	
8	2	MinX	1.	
9	2	$Q_1X$	11.5	
10	2	MedianX...	31.5	
11	21	$Q_3X$	64.	
12	22	MaxX	155.	
<div style="border: 1px solid black; padding: 2px;"> <span>C12</span> =155.         </div>				

sample standard deviation is 46.5

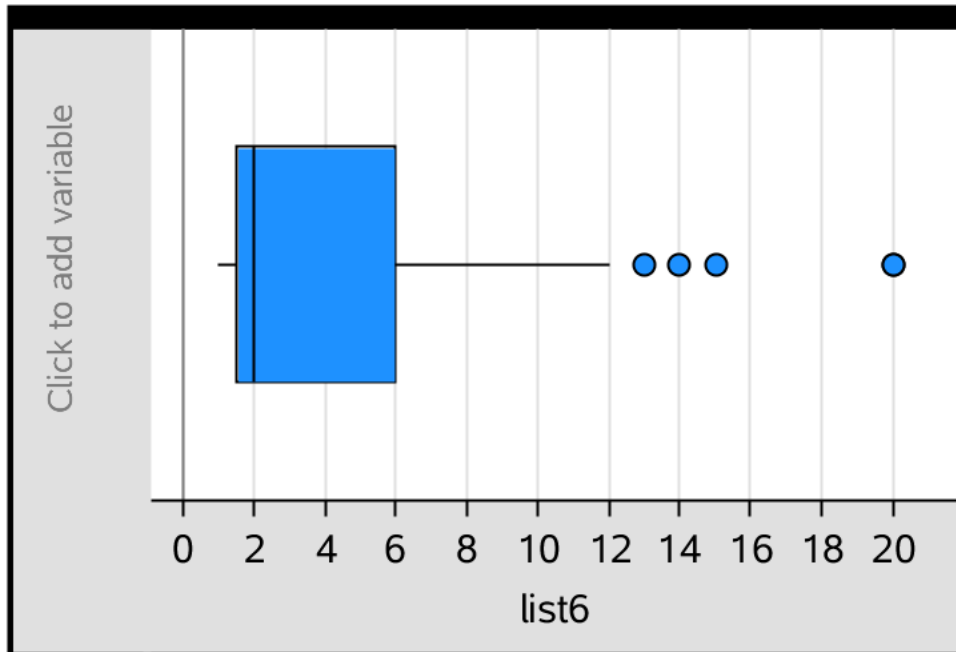
usual range

mean - 2 st dev to mean + 2 st dev

46.7 - 2 · 46.5 to 46.7 + 2 · 46.5

-46.3 to 139.7

list6

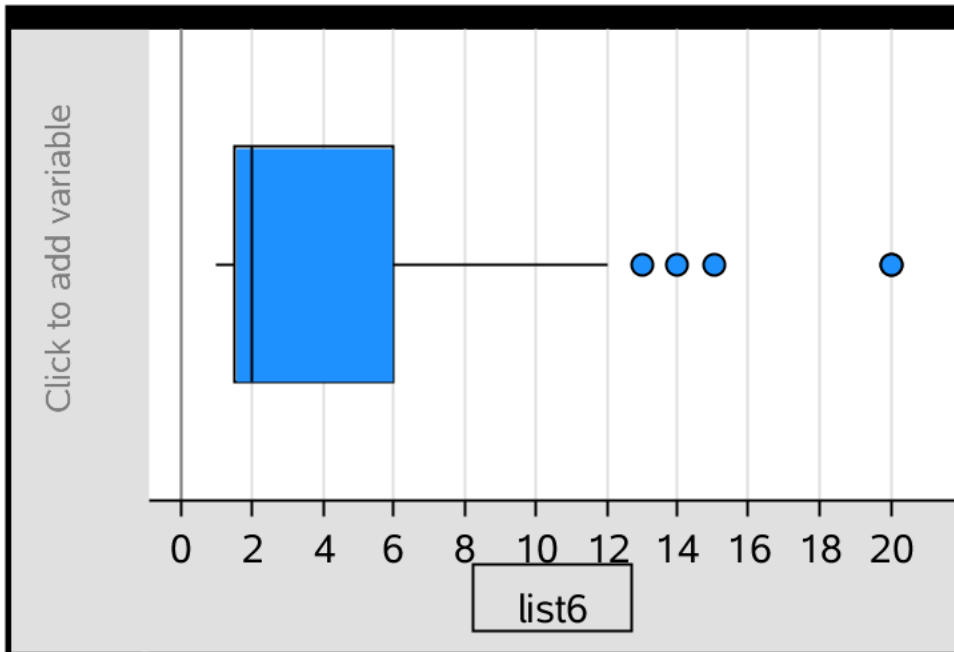


	A list6	B	C	D
=			=OneVar(	
3	1	$\Sigma x$	203.	
4	1	$\Sigma x^2$	2171.	
5	1	$s_x := s_{n-...}$	5.40839	
6	1	$\sigma_x := \sigma_{n...}$	5.34035	
7	1	n	40.	
8	1	MinX	1.	
9	1	$Q_1X$	1.5	
10	1	MedianX...	2.	
11	2	$Q_3X$	6.	
12	2	MaxX	20.	
13	2	$SSX := \Sigma..$	1140.78	

A13 =2

population variance =  $\frac{1140.78}{40.}$  ▶ 28.5195

sample variance =  $\frac{1140.78}{39.}$  ▶ 29.2508

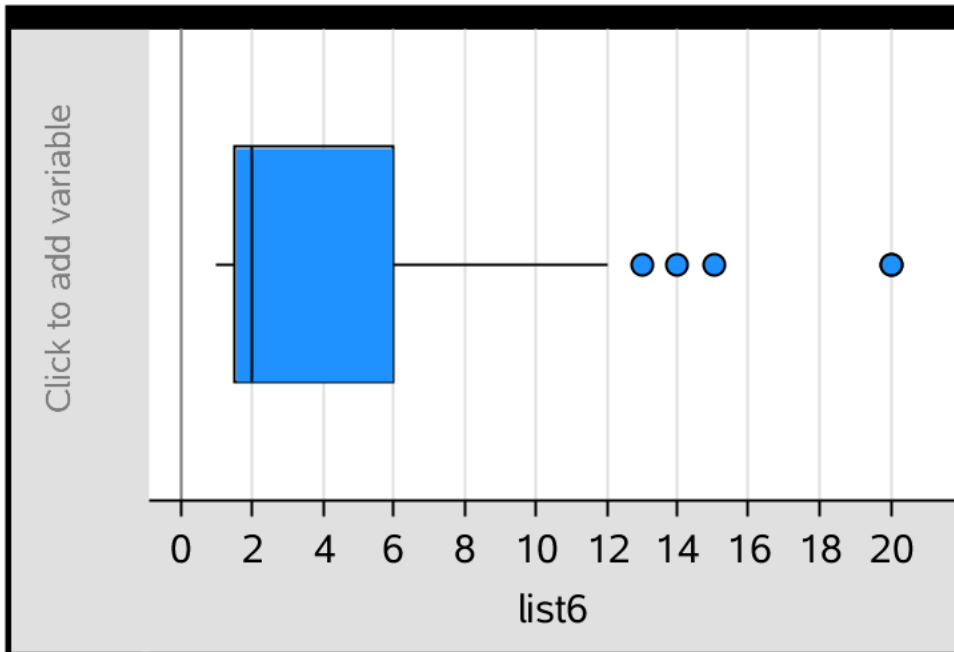


	A list6	B	C	D
=			=OneVar(	
3	1	$\Sigma x$	203.	
4	1	$\Sigma x^2$	2171.	
5	1	$s_x := s_{n-...}$	5.40839	
6	1	$\sigma_x := \sigma_{n...}$	5.34035	
7	1	n	40.	
8	1	MinX	1.	
9	1	$Q_1X$	1.5	
10	1	MedianX...	2.	
11	2	$Q_3X$	6.	
12	2	MaxX	20.	
13	2	$SSX := \Sigma..$	1140.78	
<div style="border: 1px solid black; padding: 2px;"> <span style="border-right: 1px solid black; padding-right: 5px;">C13</span> =1140.775         </div>				

$$\text{population st dev} = \sqrt{\frac{1140.78}{40.}} \rightarrow 5.34037$$

$$\text{sample st dev} = \sqrt{\frac{1140.78}{39.}} \rightarrow 5.4084$$





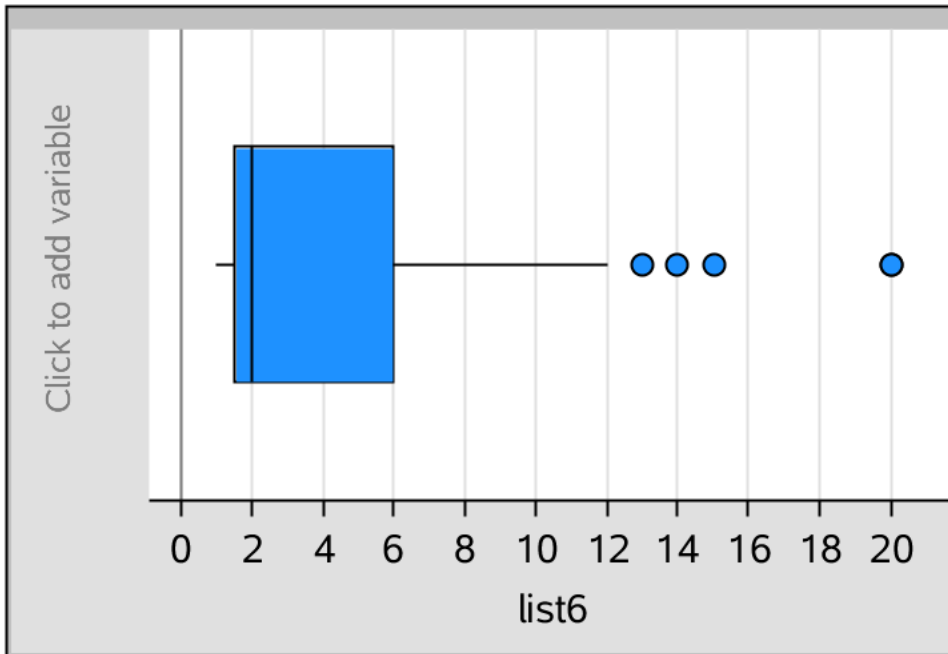
	A list6	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	5.075	
3	1	$\Sigma x$	203.	
4	1	$\Sigma x^2$	2171.	
5	1	$s_x := s_{n-...}$	5.40839	
6	1	$\sigma_x := \sigma_{n...}$	5.34035	
7	1	n	40.	
8	1	MinX	1.	
9	1	$Q_1X$	1.5	
10	1	MedianX...	2.	
11	2	$Q_3X$	6.	
C1 = "One-Variable Statistics "				

IQR =  $6 - 1.5 \blacktriangleright 4.5$

Q1 score 1.5

Q3 score 6

$1.5 \cdot \text{IQR} = 1.5 \cdot 4.5 \blacktriangleright 6.75$



	A list6	B	C	D
=			=OneVar(	
1		1 Title	One-Va...	
2		1 $\bar{x}$	5.075	
3		1 $\Sigma x$	203.	
4		1 $\Sigma x^2$	2171.	
5		1 $s_x := s_{n-...}$	5.40839	
6		1 $\sigma_x := \sigma_{n...}$	5.34035	
7		1 n	40.	
8		1 MinX	1.	
9		1 $Q_1X$	1.5	
10		1 MedianX...	2.	
11		2 $Q_3X$	6.	
C1 = "One-Variable Statistics "				

lower fence =  $1.5 - 6.75 = -5.25$

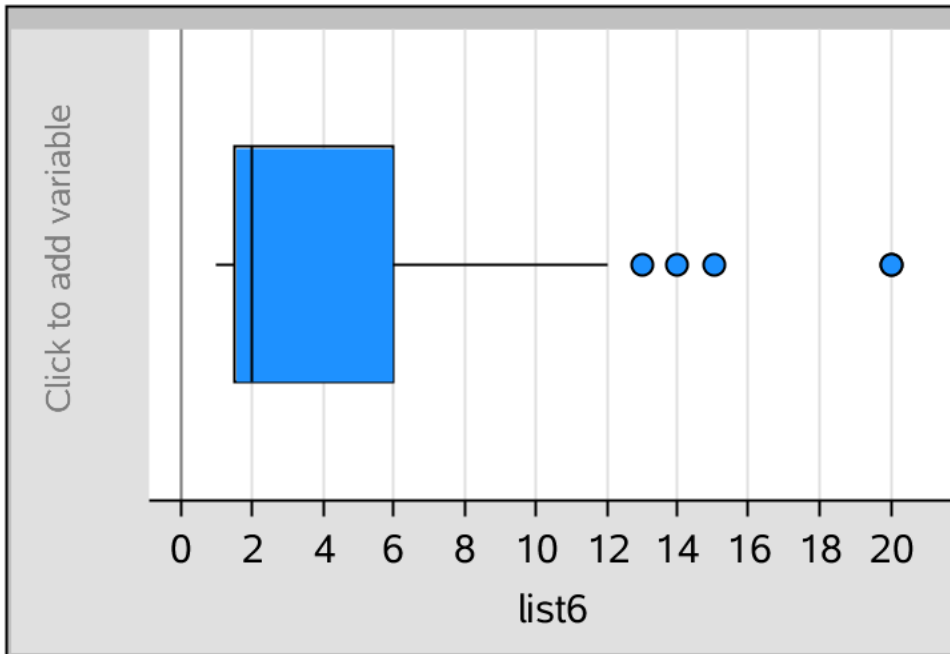
upper fence  $6 + 6.75 = 12.75$

all scores that lie

below  $x = -5.25$

and above  $x = 12.75$  are outliers

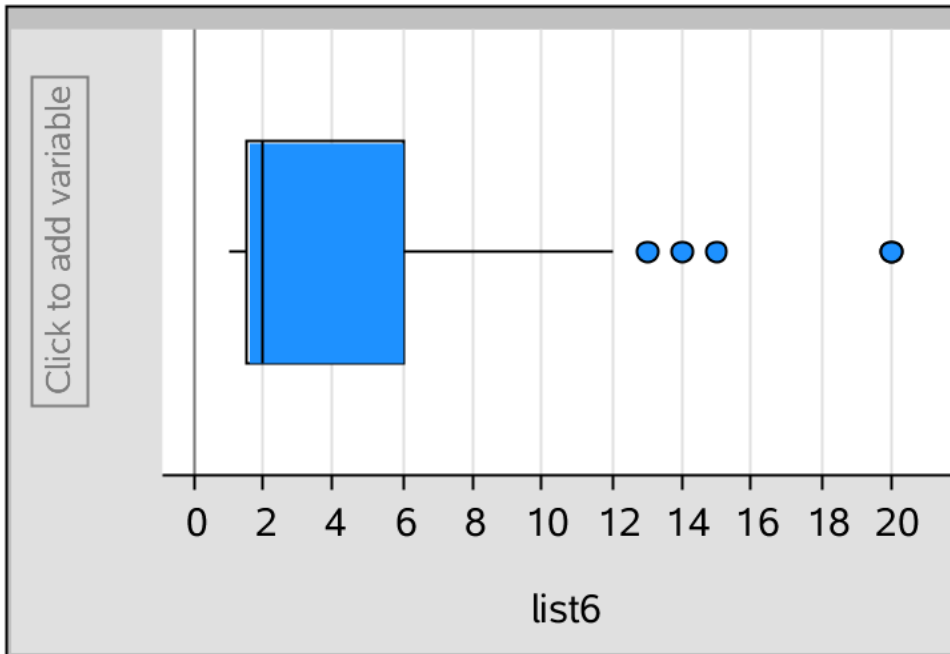
list 6 outliers 13 14 15 20



	A list6	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	5.075	
3	1	$\Sigma x$	203.	
4	1	$\Sigma x^2$	2171.	
5	1	$s_x := s_{n-...}$	5.40839	
6	1	$\sigma_x := \sigma_{n...}$	5.34035	
7	1	n	40.	
8	1	MinX	1.	
9	1	$Q_1 X$	1.5	
10	1	MedianX...	2.	
11	2	$Q_3 X$	6.	
C1 = "One-Variable Statistics "				

all scores that lie  
below  $x = -5.75$  and  
above  $x = 12.75$  are outliers

list 6 outliers are 13 14 15 20



	A list6	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	1	$\bar{x}$	5.075	
3	1	$\Sigma x$	203.	
4	1	$\Sigma x^2$	2171.	
5	1	$s_x := s_{n-...}$	5.40839	
6	1	$\sigma_x := \sigma_{n...}$	5.34035	
7	1	n	40.	
8	1	MinX	1.	
9	1	$Q_1X$	1.5	
10	1	MedianX...	2.	
11	2	$Q_3X$	6.	
A1	=1			

sample standard deviation is 5.4

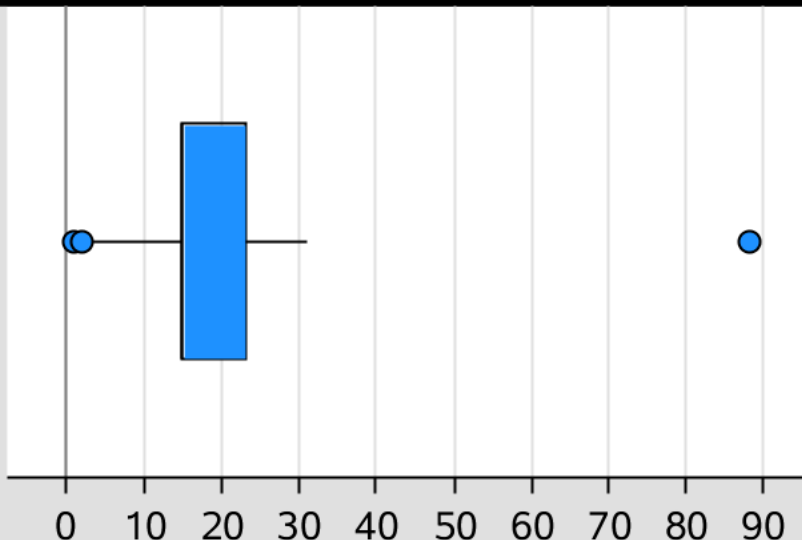
usual range

mean - 2 st dev to mean + 2 st dev

5.1-2·5.4 to 5.1+2·5.4

-5.7 to 15.9

list7



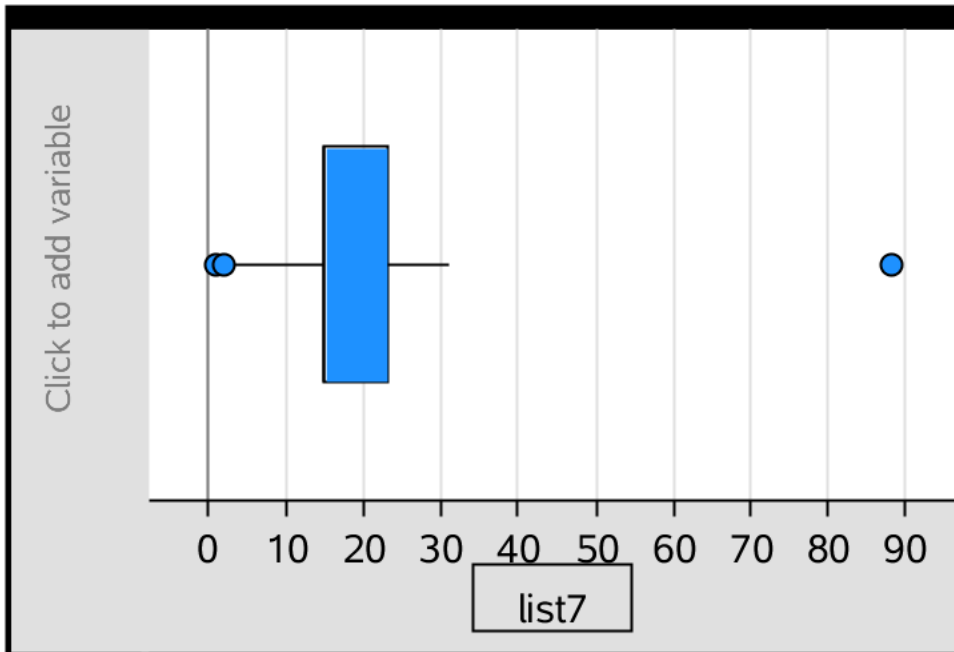
list7

population variance =  $\frac{7729.6}{40.}$  ▶ 193.24

sample variance =  $\frac{7729.6}{39.}$  ▶ 198.195

	A list7	B	C	D
=			=OneVar(	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	Q <sub>1</sub> X	15.	
10	15	MedianX...	15.	
11	15	Q <sub>3</sub> X	23.	
12	15	MaxX	88.	
13	15	SSX := $\Sigma..$	7729.6	

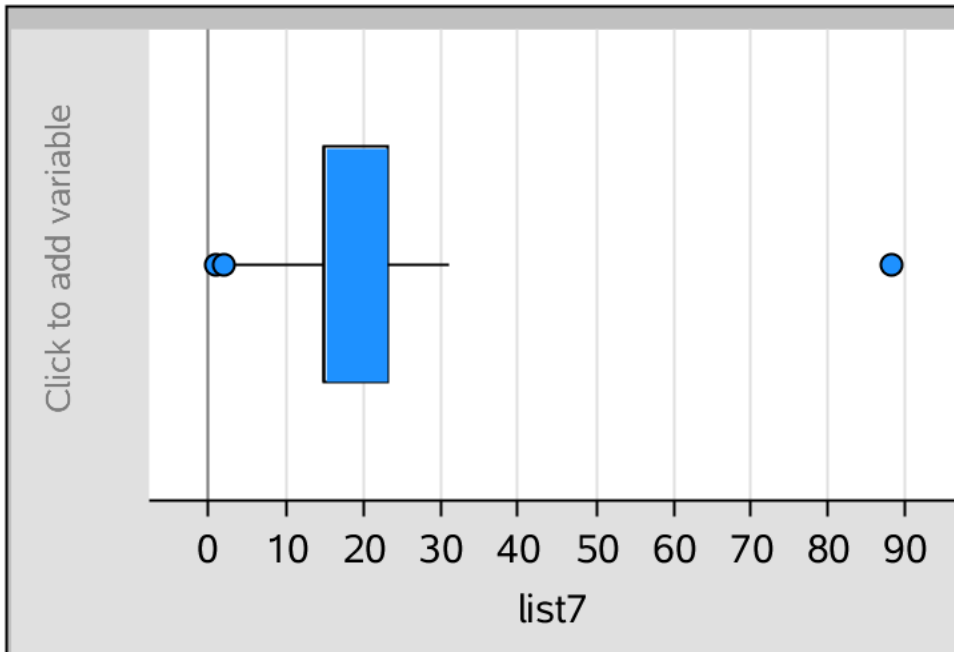
C13 =7729.6



	A list7	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	2	$\bar{x}$	18.4	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	Q <sub>1</sub> X	15.	
10	15	MedianX...	15.	
11	15	Q <sub>3</sub> X	23.	
C1 = "One-Variable Statistics "				

population st dev =  $\sqrt{\frac{7729.6}{40.}}$  ▶ 13.9011

sample st dev =  $\sqrt{\frac{7729.6}{39.}}$  ▶ 14.0782



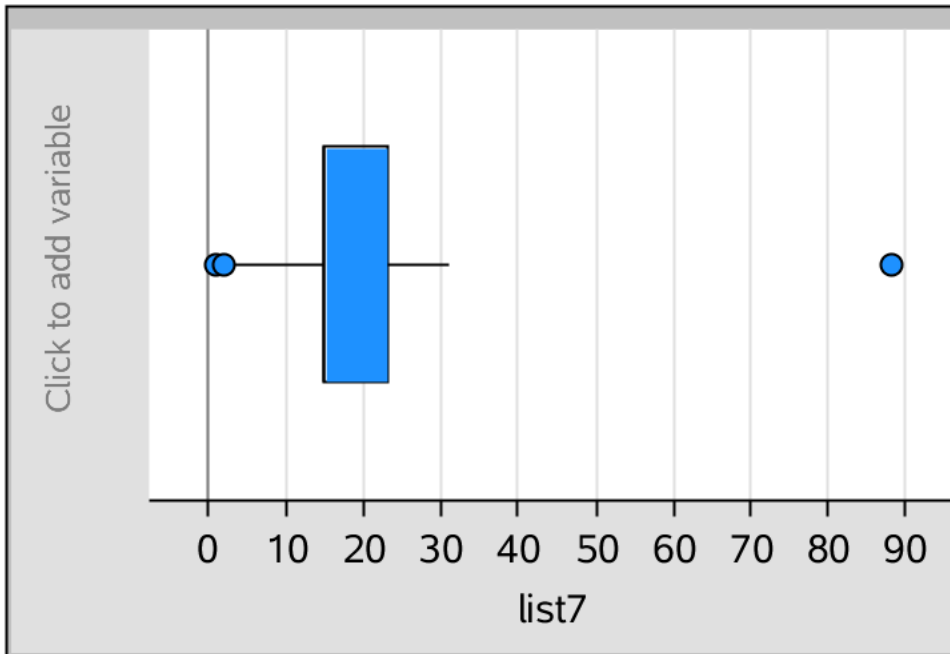
IQR =  $23 - 15 \blacktriangleright 8$

Q1 score 15

Q3 score 23

$1.5 \cdot \text{IQR} = 1.5 \cdot 8 \blacktriangleright 12.$

	A list7	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	2	$\bar{x}$	18.4	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	$Q_1 X$	15.	
10	15	MedianX...	15.	
11	15	$Q_3 X$	23.	
C1 = "One-Variable Statistics "				



	A list7	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	2	$\bar{x}$	18.4	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	$Q_1X$	15.	
10	15	MedianX...	15.	
11	15	$Q_3X$	23.	
C1 = "One-Variable Statistics "				

lower fence =  $15 - 12 = 3$

upper fence  $23 + 12 = 35$

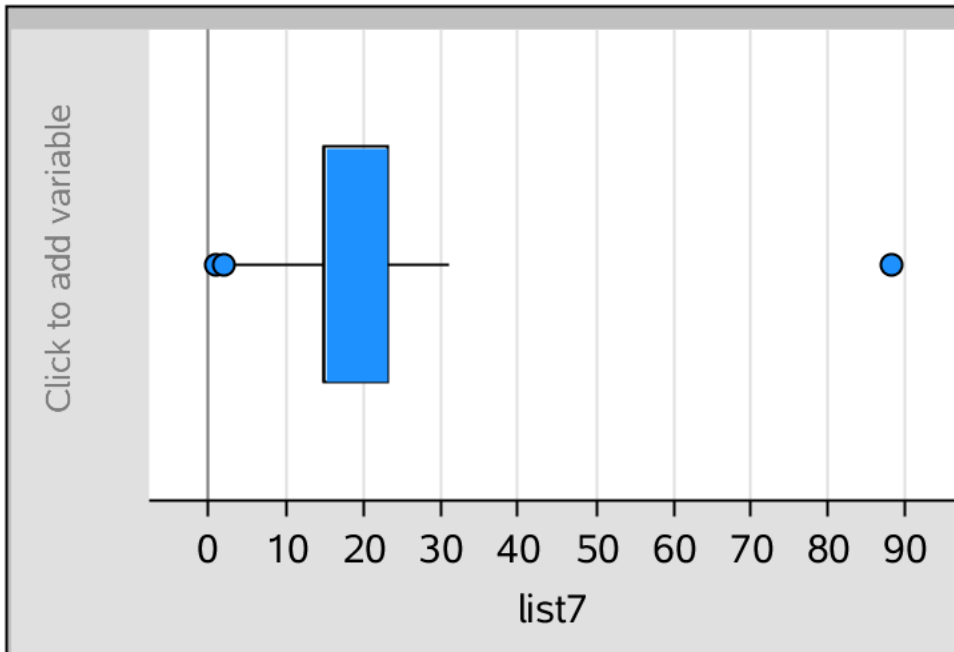
all scores that lie

below  $x = 3$

and above  $x = 35$  are outliers

list 7 outliers 1 2 88

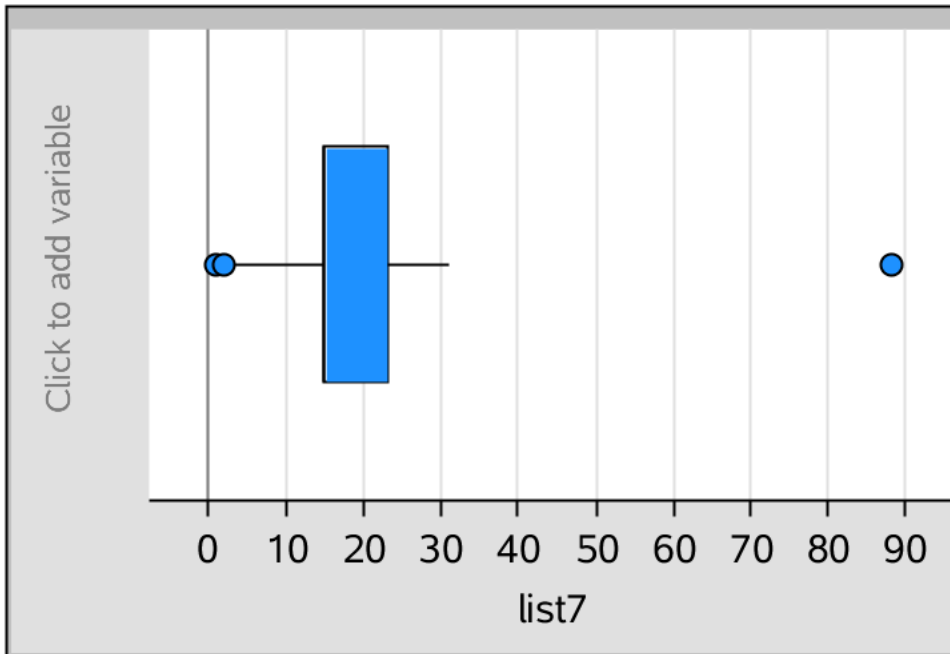




all scores that lie  
 below  $x = 3$  and  
 above  $x = 35$  are outliers

list 7 outliers are 1 2 88

	A list7	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	2	$\bar{x}$	18.4	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	$Q_1X$	15.	
10	15	MedianX...	15.	
11	15	$Q_3X$	23.	
A2	=2			



	A list7	B	C	D
=			=OneVar(	
1	1	Title	One-Va...	
2	2	$\bar{x}$	18.4	
3	3	$\Sigma x$	736.	
4	4	$\Sigma x^2$	21272.	
5	5	$s_x := s_{n-...}$	14.0782	
6	6	$\sigma_x := \sigma_{n...}$	13.9011	
7	7	n	40.	
8	15	MinX	1.	
9	15	$Q_1 X$	15.	
10	15	MedianX...	15.	
11	15	$Q_3 X$	23.	
C1 = "One-Variable Statistics "				

sample standard deviation is 14.1

usual range

mean - 2 st dev to mean + 2 st dev

18.4 - 2 · 14.1 to 18.4 + 2 · 14.1

-9.8 to 46.6

### Empirical Rule

List 5

68% of the data should lie between  
mean - 1 st dev to mean + 1 st dev

$$46.7 - 1 \cdot 46.5 \quad \text{to} \quad 46.7 + 1 \cdot 46.5$$

$$46.7 - 2 \cdot 46.5 \quad \blacktriangleright \quad -46.3 \quad \text{to}$$

$$46.7 + 2 \cdot 46.5 \quad \blacktriangleright \quad 139.7$$

### Empirical Rule

list 5

95% of the data should lie between  
usual range

mean - 2 st dev to mean + 2 st dev

$$46.7 - 2 \cdot 46.5 \quad \text{to} \quad 46.7 + 2 \cdot 46.5$$

$$-46.3 \quad \text{to} \quad 139.7$$

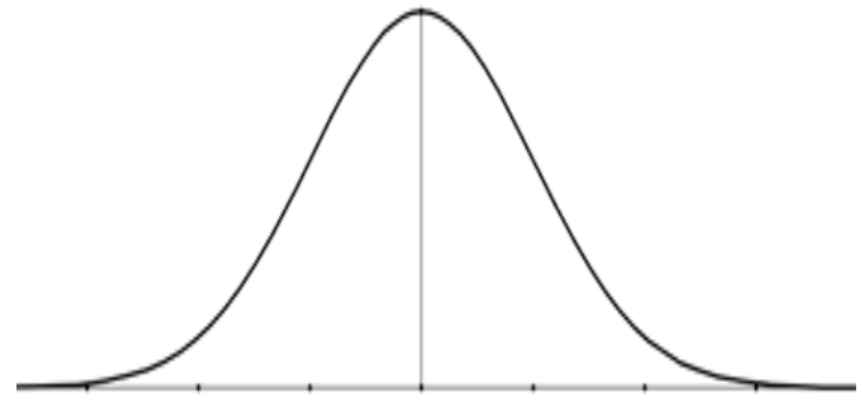
### Empirical Rule

List 5

99.7% of the data should lie between  
mean - 3 st dev to mean + 3 st dev

$$46.7 - 3 \cdot 46.5 \quad \text{to} \quad 46.7 + 3 \cdot 46.5$$

$$-92.8 \quad \text{to} \quad 186.2$$



### Empirical Rule

List 6

68% of the data should lie between  
mean - 1 st dev to mean + 1 st dev

$$5.1 - 1 \cdot 5.4 \text{ to } 5.1 + 1 \cdot 5.4$$

$$-0.3 \text{ to } 10.5$$

### Empirical Rule

list 6

95% of the data should lie between  
usual range

$$\text{mean} - 2 \text{ st dev to mean} + 2 \text{ st dev}$$

$$5.1 - 2 \cdot 5.4 \text{ to } 5.1 + 2 \cdot 5.4$$

$$-5.7 \text{ to } 15.9$$

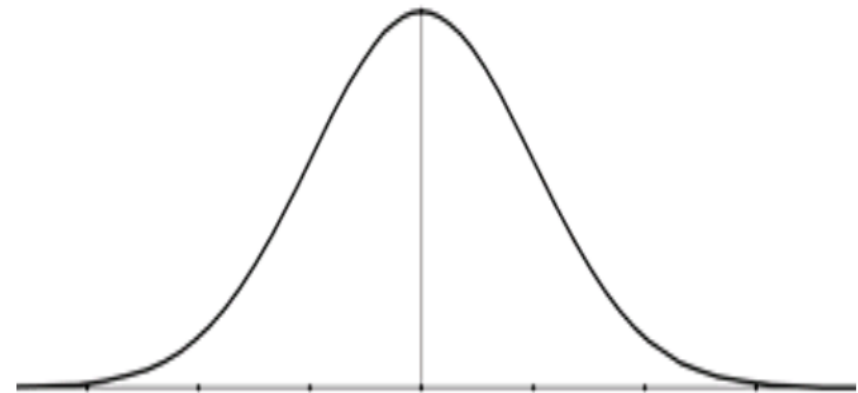
### Empirical Rule

List 6

99.7% of the data should lie between  
mean - 3 st dev to mean + 3 st dev

$$5.1 - 3 \cdot 5.4 \text{ to } 5.1 + 3 \cdot 5.4$$

$$-11.1 \text{ to } 21.3$$



### Empirical Rule

List 7

68% of the data should lie between  
mean - 1 st dev to mean + 1 st dev

$$18.4 - 1 \cdot 14.1 \quad \text{to} \quad 18.4 + 1 \cdot 14.1$$

$$4.3 \quad \text{to} \quad 32.5$$

### Empirical Rule

list 7

95% of the data should lie between  
usual range

$$\text{mean} - 2 \text{ st dev to mean} + 2 \text{ st dev}$$

$$18.4 - 2 \cdot 14.1 \quad \text{to} \quad 18.4 + 2 \cdot 14.1$$

$$-9.8 \quad \text{to} \quad 46.6$$

### Empirical Rule

List 7

99.7% of the data should lie between  
mean - 3 st dev to mean + 3 st dev

$$18.4 - 3 \cdot 14.1 \quad \text{to} \quad 18.4 + 3 \cdot 14.1$$

$$-23.9 \quad \text{to} \quad 60.7$$

